

## Abstract of the Disclosure

A method authenticates  $d_i$  identities in parallel using two prime numbers  $p$  and  $q$  such that  $q \mid p - 1$ . Each identity includes a private key  $s_i$  and a public key  $v_i$ , and a publicly known generator is  $\alpha$  such that  $\alpha^q \equiv 1 \pmod{p}$ . A verifier is provided with an ordered list of the public keys  $v_i$ . A prover selects uniformly at random a non-negative number  $r$  less than  $q$ . A number  $x = \alpha^r \pmod{p}$  is sent from the prover to a verifier. The verifier selects uniformly at random a non-negative number  $e$  less than  $2^{(t+\log d)}$ , where  $\log$  is base 2, and a number  $t$  is a predetermined security parameter. The prover receives from the verifier the number  $e$ . A number  $y = r + \sum_i s_i * e^i \pmod{q}$  is generated by the prover, and the number  $Y$  is sent to the verifier, who then determines if an equality  $x = \alpha^y * \prod_i (v_i)^{e^i} \pmod{p}$  is true. The prover is accepted as having the  $d_i$  identities if and only if the equality is true. In a preferred embodiment the communications between the prover and the verifier is via a low-bandwidth optical channel.